It Show that the uniform limit of  
a sequence of contain on functions  
is containous, and hence that if 
$$m(E) < +\infty$$
  
and  $f: E \to |R|$  to measurable then,  $\forall \eta > 0$ ,  
 $\exists closed set F \subseteq E with  $m(E \setminus F) < \eta$   
mit that  $f|_F : F \to |R|$  to continuous.$ 

2. Let 
$$F = \bigcup_{n=1}^{n} F_n$$
, dijont closed sets  $F_{i}, ..., F_n$ .  
Let  $f: F \rightarrow IR$  he such that  $f|_{F_n}$  is  $ct_{5}, \forall n$ .  
Show that  $f$  is  $ct_{5}$ .  
3.\* Let  $F_n \subseteq (n, n+1]$  be closed ( $IR : F_n$   
of  $m$ )  $\forall n \in N$ , and let  $F = \bigcup_{n \in N} F_n$ .  
Show that  $f: F \rightarrow IR$  is continuous if  
each  $f|_{F_n}$  is  $ct_{5}$ . (Can the condition  
 $F_n \subseteq (n, n+1]$  be weakened to  $F_n \subseteq IR$ ?)

4. Let  $G = \bigcup_{n \ge 1} I_n$ , comtable disjoint open interrets In, and let F: IRIG. Let X<Y<Z with X,ZEF and YEIn=(an,bn). Show hart an EF, bn EF, XSan, and bn SJ 5. Let G, In, F he as in Q4, and let f: IR->IR be such that  $J|_F$  and  $f|_{\overline{In}}$  be contrinuous, YnEN (In denotes the closure of In). Suppose further Xhat the graph of  $f|_{\overline{T}}$  is a line-segment. Show that f is contininous ( by symmetry, need my show that f is right-containing at  $each x_{0} \in |\mathbb{R} := \lim_{x \to x_{0} \neq x_{0}} f(x) = f(x_{0}), i.e. \forall \xi = 70 \exists$   $\chi \to \chi_{0} \neq x_{0} \neq x$ This is evident if 26EG (So InENSIF Xo (-In). We may hence assume that xo EF, and true are three cases to consider